

## Lesson 1.4: Linear Inequalities

# What is an Inequality?

It is an equation that instead of an "=", it has one of the following:

$<$ ,  $>$ ,  $\leq$ ,  $\geq$

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Inequalities have one of the following:

$<$ ,  $>$ ,  $\leq$ ,  $\geq$

To "solve" means to find all values of the variable for which the statement is true.

The values are called *Solutions*. The set of all solutions is called the *solution set*.

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Give me three examples of inequalities:

1.

2.

3.

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When we find the solution, we can put the answers in **SET NOTATION** (like we've done before), or in something called **INTERVAL NOTATION**.

**Practice Set Notation:**

EX: Write  $x = 5$  in set notation.

EX: Write  $x > 5$  in set notation.

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### *Interval Notation*

Assume  $a < b$  where  $a$  and  $b$  are real numbers.

#### Closed Interval:

denoted by  $[a, b]$ , consists of all real numbers  $x$  for which  $a \leq x \leq b$ .

#### Open Interval:

denoted by  $(a, b)$ , consists of all real numbers  $x$  for which  $a < x < b$ .

#### Half-Open, Half-Closed Intervals:

denoted by  $(a, b]$  for all real numbers  $x$  for which  $a < x \leq b$  and  $[a, b)$  for all real numbers  $x$  for which  $a \leq x < b$ .

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### Interval Notation cont:

If we have  $(a, b)$  or  $(a, b]$  or  $[a, b)$ , then:

"a" is called the left end point.

"b" is called the right end point.

Name the end points of the following:

a.)  $(3, 5)$

b.)  $[-2, 5]$

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What if we don't have an end point?










For example:  $x > 4$

It just goes on forever.... What number is "forever"? Can you think of one?

Write in interval notation:

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### Intervals including $\infty$ :

$(a, b)$	$\{x \mid a < x < b\}$	
$[a, b]$	$\{x \mid a \leq x \leq b\}$	
$[a, b)$	$\{x \mid a \leq x < b\}$	
$(a, b]$	$\{x \mid a < x \leq b\}$	
$[a, \infty)$	$\{x \mid x \geq a\}$	
$(a, \infty)$	$\{x \mid x > a\}$	
$(-\infty, a]$	$\{x \mid x \leq a\}$	
$(-\infty, a)$	$\{x \mid x < a\}$	
$(-\infty, \infty)$	$\{x \mid x \text{ is a real number}\}$	



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Let's do some examples.

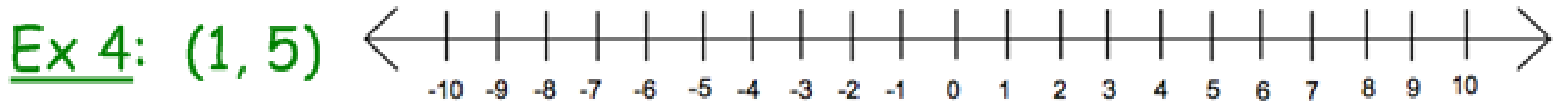
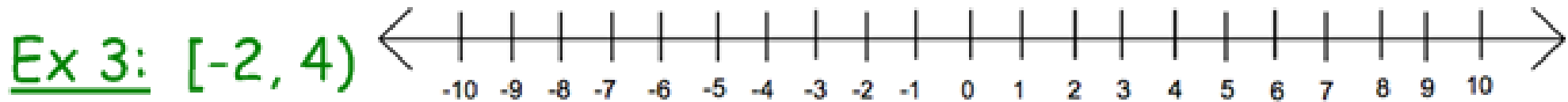
Write in interval notation.

EX 1:  $-2 \leq x \leq 4$

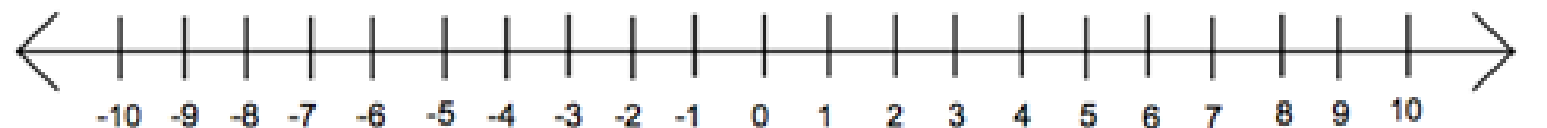
EX 2:  $1 < x \leq 5$

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Write in Inequality notation and graph



Ex 5:  $[-5, \infty)$



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If we have  $5 > 3$ ,

What would happen if we added 6 to both sides?  
Would the inequality still be true?

Would it still be true if we subtract 4 from both sides?

If we have  $2 < 7$ ,

Would the inequality still be true IF we add 6 to both sides?

What if we subtract 4 from both sides?

A general way to say this is if we have ***a***, ***b***, and ***c***, then we have

1. if  $a > b$ , then  $a+c > b+c$  and  $a-c > b-c$
2. if  $a < b$ , then  $a+c < b+c$  and  $a-c < b-c$

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If we have  $4 > 1$ ,

What would happen if we multiplied by 6 on both sides?  
Would the inequality still be true?

Would it still be true if we divided by 4 on both sides?

If we have  $-1 < 3$ ,

Would the inequality still be true IF we multiplied by 6 on both sides?

What if we divided by 3 on both sides?

A general way to say this is if we have  $a$ ,  $b$ , and  $c$ , then we have

1. if  $a > b$ , then  $a \cdot c > b \cdot c$  and  $a/c > b/c$
2. if  $a < b$ , then  $a \cdot c < b \cdot c$  and  $a/c < b/c$

## Lesson 1.4: Linear Inequalities

Let's solve some examples and then graph them. (Watch out for those negatives! *What should you do if to the  $</>$  if you divide or multiply by a negative?*) *Write answers in Set notation and Interval Notation.*

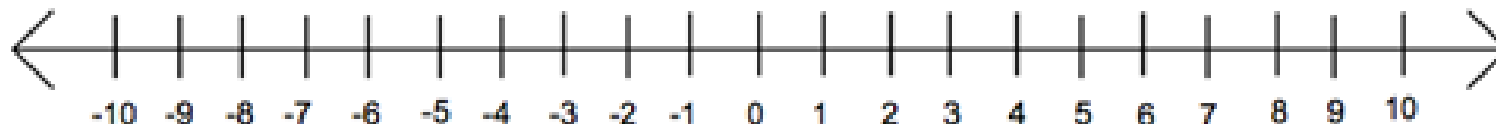
1.  $6x + 3 > 5x - 2$



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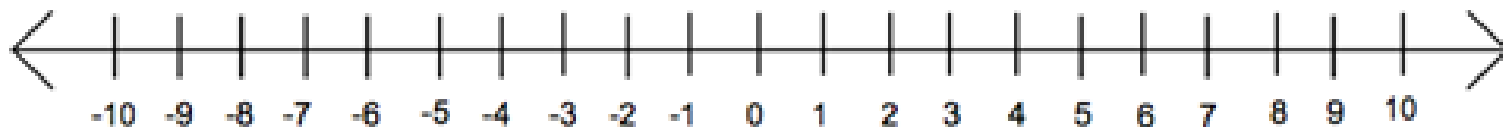
2.  $-3x - 4 < 14$



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Let's solve some examples and then graph them. (Watch out for those negatives! *What should you do if to the  $</>$  if you divide or multiply by a negative?*) *Write answers in Set notation and Interval Notation.*

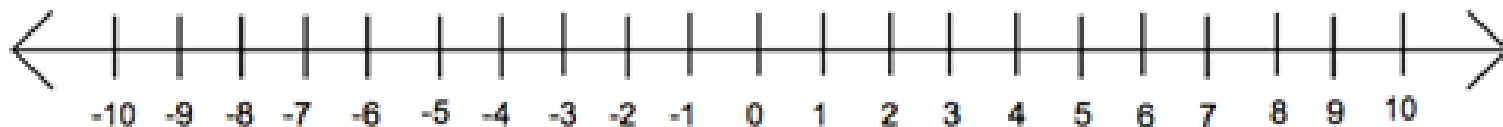
3.  $-3(4x + 7) < 21$



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Let's solve some examples and then graph them. (Watch out for those negatives! *What should you do if to the  $</>$  if you divide or multiply by a negative?*) *Write answers in Set notation and Interval Notation.*

$$4. \frac{2x + 1}{3} > \frac{x - 2}{2}$$





Lesson 1.4: Linear Inequalities

Homework:

Pg. 97: 4-8 all, 9-27 odds, 32-36 evens,  
61, 67, 74

(21 problems)

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Homework: Alternative

Pg 97: # 4-8 all, 9-27 odds, 32-36  
(evens), 61, 67, 74

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