

We will be able to:

1. Graph linear equations by plotting points.
2. Graph linear equations by intercepts.
3. Graph vertical and horizontal lines.
4. Applications of Linear Equations.

Lesson 3.1: Linear Equations and Functions

Linear Equation:

A Linear equation in two variable (in Standard Form) looks like this

$$Ax + By = C$$

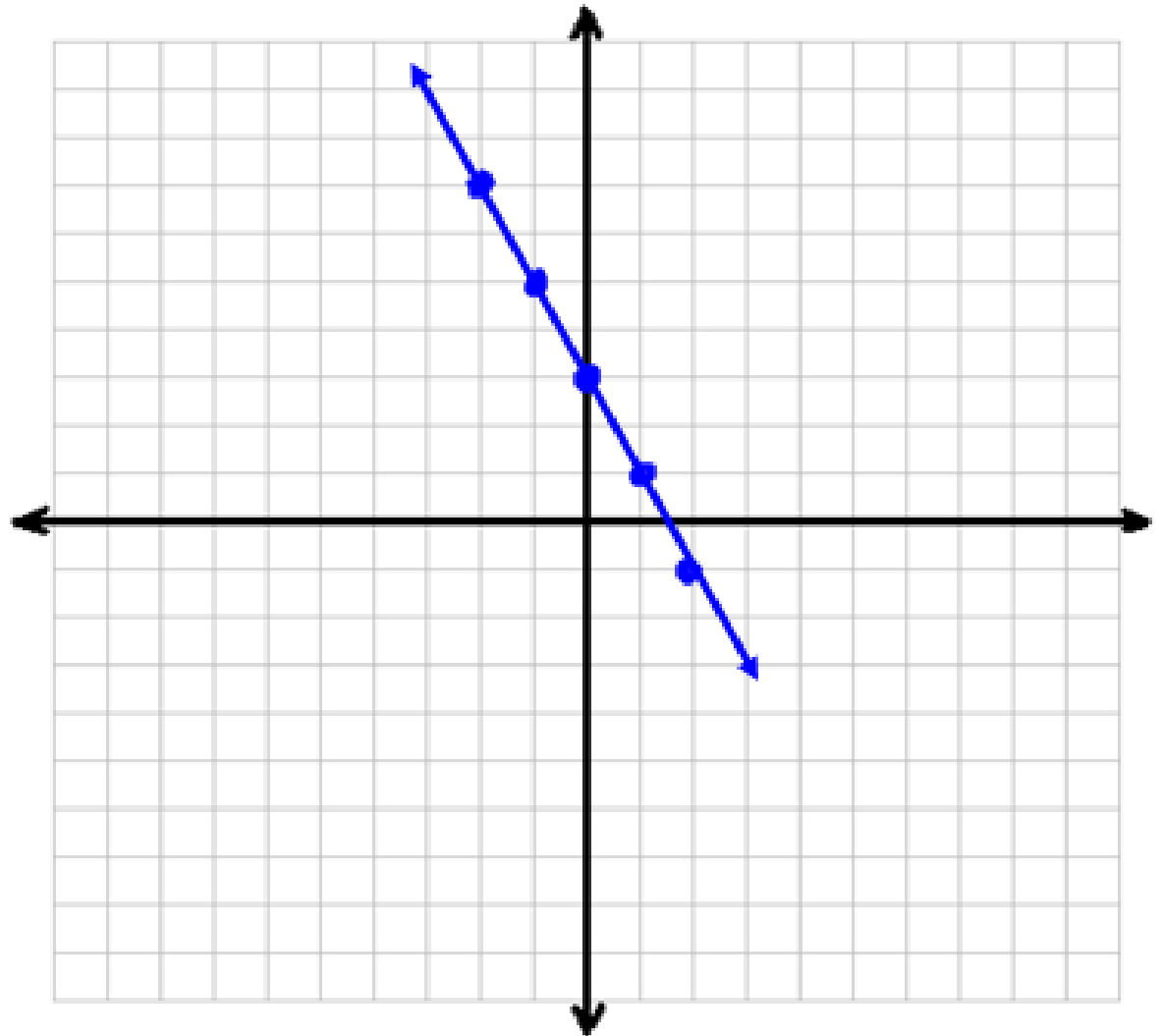
where A , B , and C are real numbers. A and B cannot BOTH be 0.

Lesson 3.1: Linear Equations and Functions

Graph by Plotting Points:

Example 1: $4x + 2y = 6 \rightarrow 2y = -4x + 6 \rightarrow y = -2x + 3$

x	$y = -2x + 3$
-2	$7 = -2(-2) + 3$
-1	$5 = -2(-1) + 3$
0	$3 = -2(0) + 3$
1	$1 = -2(1) + 3$
2	$-1 = -2(2) + 3$



Graph by Intercepts:

We can graph a line by finding the X and Y intercepts. We find each, plot, connect the dots and, voila, we have a line. :)

Here's how:

X-Intercept: Let $y = 0$ in the equation and then solve for x .
This is your x - intercept.

Y- Intercept: Let $x = 0$ in the equation and then solve for y .
This is your y - intercept.

Lesson 3.1: Linear Equations and Functions

Graph by Intercepts:

Example 2: $3x + 2y = 12$

x-int: $(4, 0)$

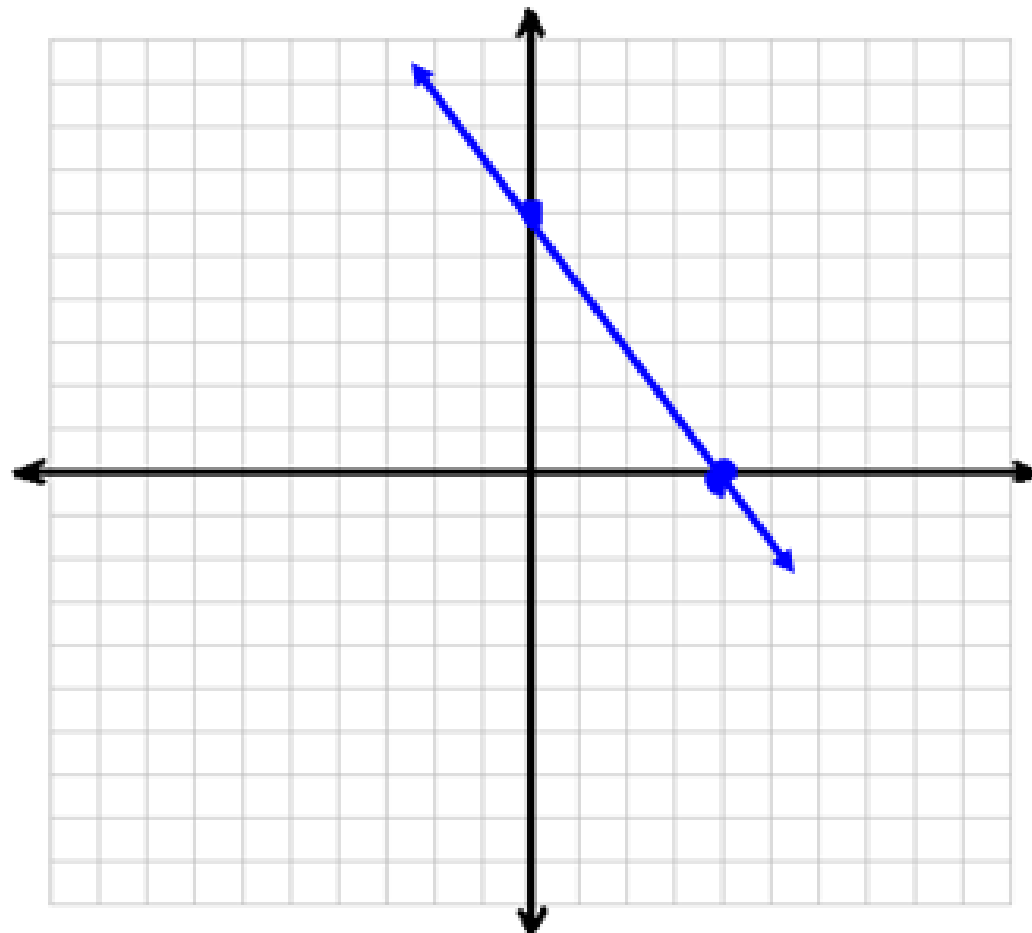
$$\frac{3x}{3} = \frac{12}{3}$$

$$x = 4$$

y-int: $(0, 6)$

$$2y = 12$$

$$y = 6$$



Lesson 3.1: Linear Equations and Functions

Graph by Intercepts:

Example 3: $4x - 5y = 20$

x-int: $(5, 0)$

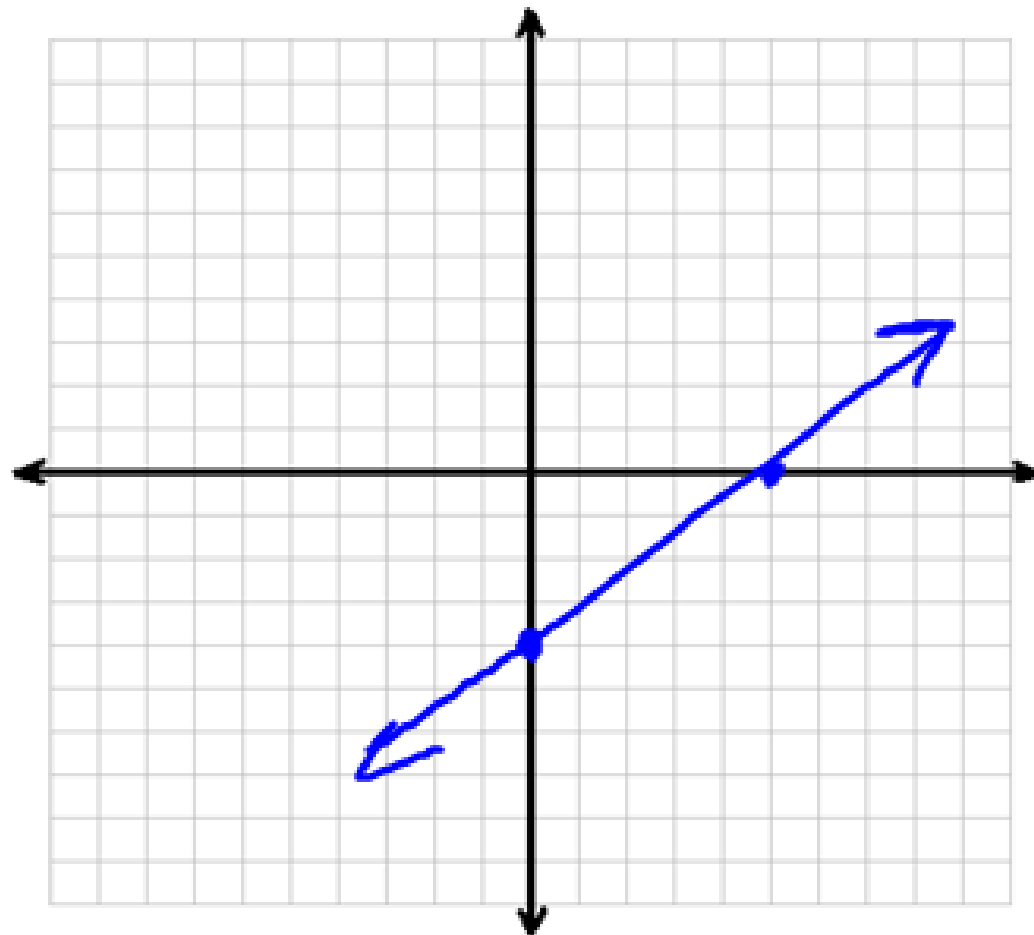
$$4x = 20$$

$$x = 5$$

y-int: $(0, -4)$

$$-5y = 20$$

$$y = -4$$



Lesson 3.1: Linear Equations and Functions

Graph by Intercepts:

Example 4: $x + 3y = 0$

x-int: $(0, 0)$

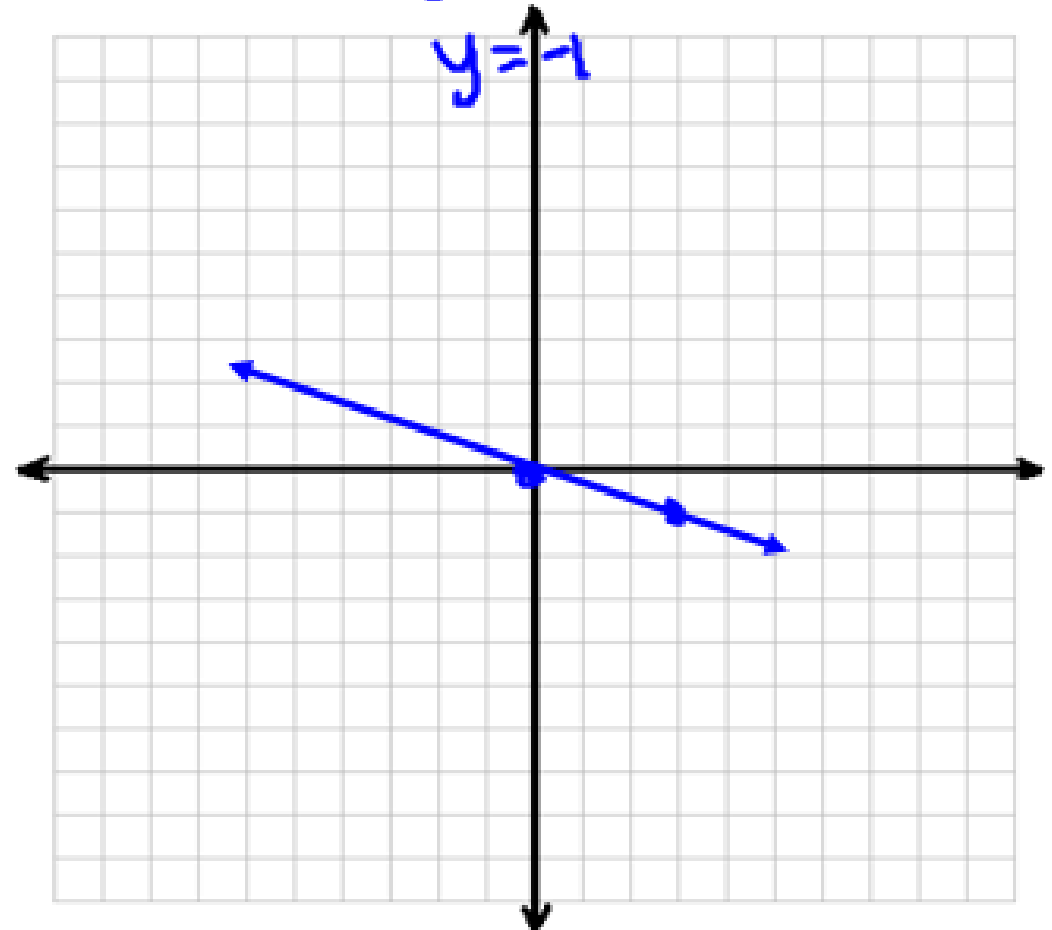
$$x = 0$$

y-int: $(0, 0)$

$$3y = 0$$

$$y = 0$$

$$\begin{array}{r} \text{pick } x=3 \\ \hline 3 + 3y = 0 \\ -3 \quad \quad -3 \\ \hline 3y = -3 \\ \frac{3y}{3} = \frac{-3}{3} \end{array} \quad (3, -1)$$

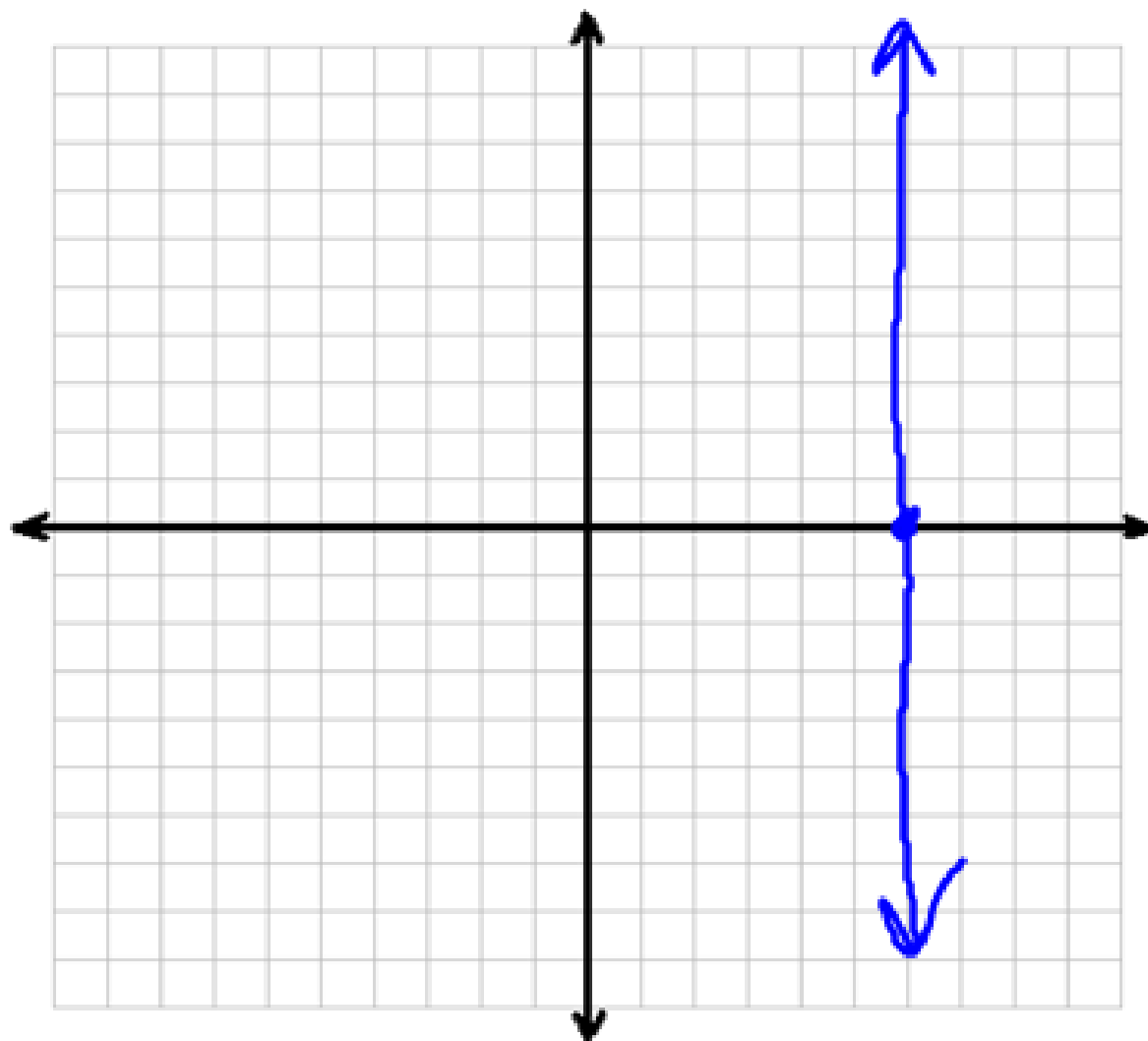


Lesson 3.1: Linear Equations and Functions

Graph by Plotting Points:

Example 5: $x = 6$

x	y
6	0
6	2
6	1
6	-1
6	-2

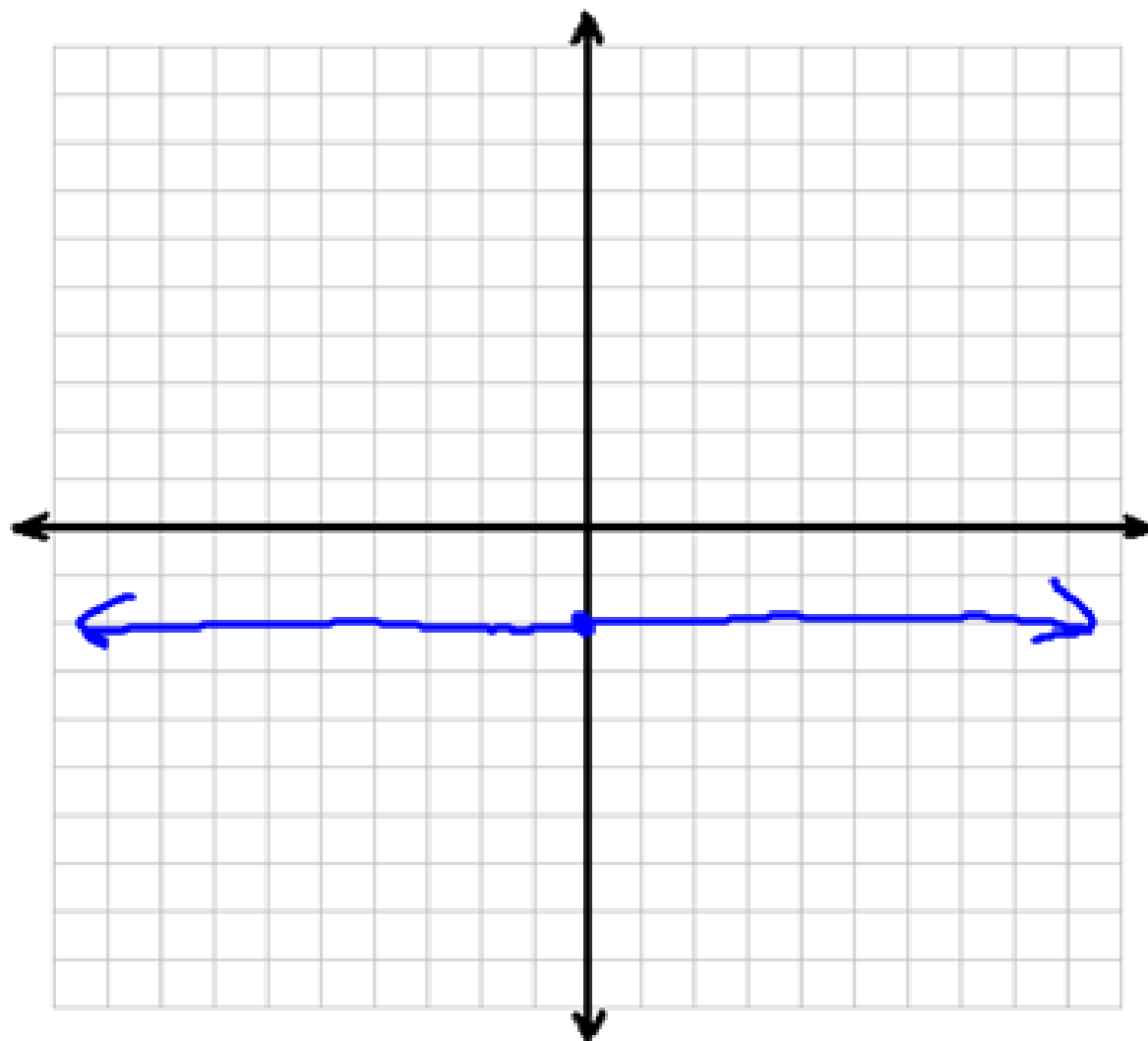


Lesson 3.1: Linear Equations and Functions

Graph by Plotting Points:

Example 6: $y = -2$

x	y
0	-2
-3	-2
15	-2



Lesson 3.1: Linear Equations and Functions

A Vertical Line is given by an equation of the form

$$\underline{x = a}$$

where a is the x - intercept.

A Horizontal Line is given by an equation of the form

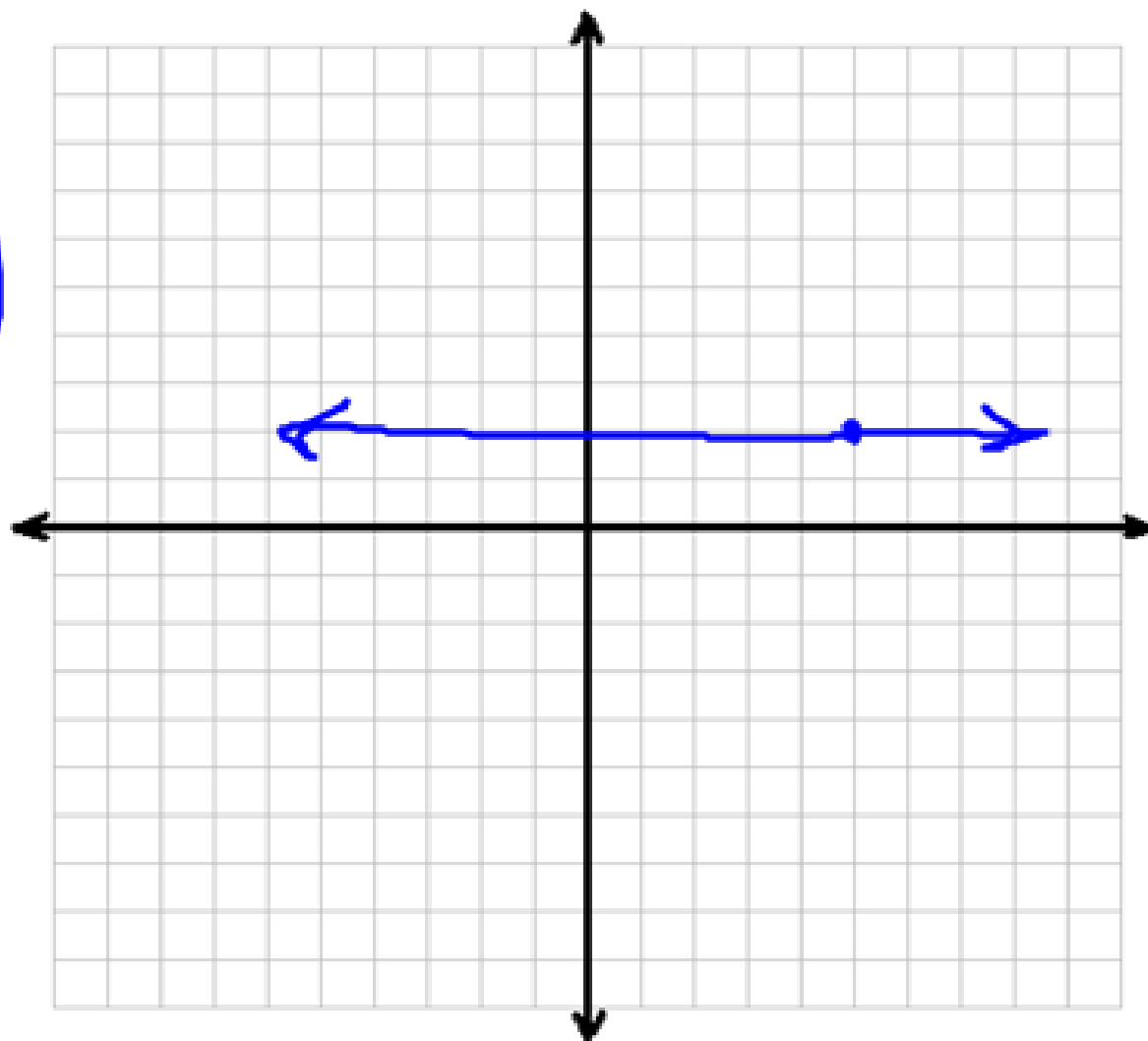
$$\underline{y = b}$$

where b is the y - intercept.

Lesson 3.1: Linear Equations and Functions

Example 7: Write an equation of a horizontal line that goes through the point $(5, \underline{2})$ and graph.

$$y = 2$$



Lesson 3.1: Linear Equations and Functions

Definition:

A Linear Function is a function of the form

$$f(x) = mx + b$$

where m and b are real numbers. The graph of a linear function is called a *line*.

Lesson 3.1: Linear Equations and Functions

Applications:

Example 8: Tony's weekly salary at Apple Chevrolet is 0.75% of his weekly sales plus \$450. The linear function

$$S(x) = 0.0075x + 450$$

describes Tony's weekly salary, S , as a linear function of his weekly sales, x .

a.) What is the implied Domain?

$$[0, \infty)$$

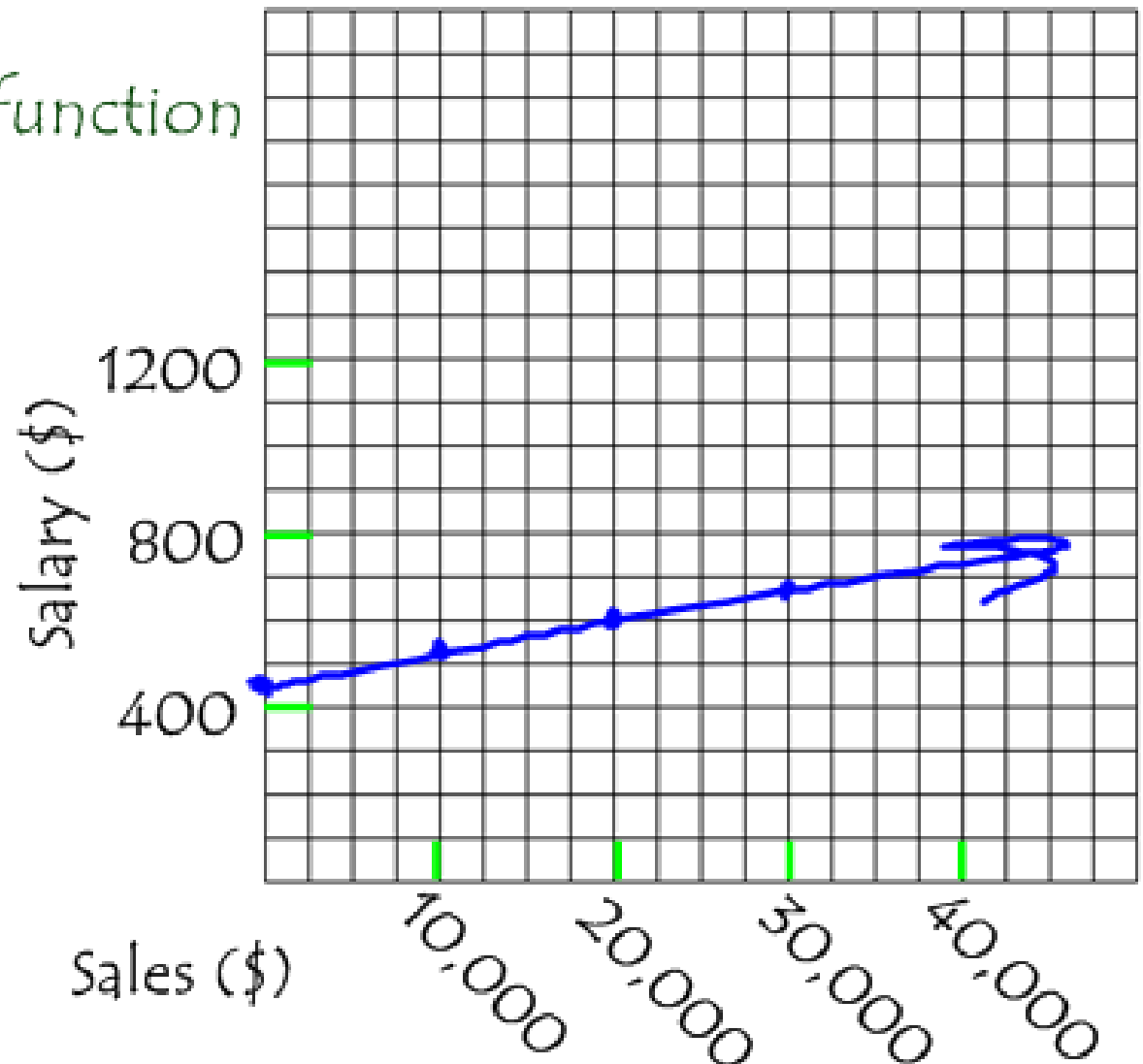
Lesson 3.1: Linear Equations and Functions

Example 8: Tony's weekly salary at Apple Chevrolet

$$S(x) = 0.0075x + 450$$

b.) Draw a graph of the function

x	$y = S(x)$
0	450
10,000	525
20,000	600
30,000	675



Lesson 3.1: Linear Equations and Functions

Example 8: Tony's weekly salary at Apple Chevrolet

$$S(x) = 0.0075x + 450$$

c.) If Tony sells cars worth a total of \$42,000 in one week, what is his salary?

$$S(42,000) = .0075(42,000) + 450$$

$$S(42,000) = 765$$

His salary is \$765 for the week.

d.) If Tony earned \$840 one week, what was the value of the cars that he sold?

$$\begin{array}{r} 840 = .0075x + 450 \\ -450 \qquad -450 \\ \hline \end{array}$$

$$\begin{array}{r} 390 = .0075x \\ \underline{.0075} \qquad \underline{.0075} \end{array} \rightarrow x = 52,000$$

The value of the cars he sold was \$52,000.

Lesson 3.1: Linear Equations and Functions

Homework:

Pg. 196: #'s 4-8 all, 13, 15, 17,
21, 27, 31, 35-49 odds
(18 problems)