

Algebra 2 - Assignment 16

NEW

p259: 5. $3wz^{-4} = \frac{3w}{z^4}$

13. $\left(\frac{bc}{2}\right)^{-3} = \frac{2^3}{(bc)^3} = \frac{8}{bc^3}$

25. $(a^3b^3)(ab)^{-2} = a^3b^3a^{-2}b^{-2} = a^{3-2}b^{3-2} = ab$

43. $\frac{40a^{-1}b^{-7}}{20a^{-5}b^{-9}} = \frac{40}{20} \cdot a^{-1-(-5)}b^{-7-(-9)} = 2a^{-1+5}b^{-7+9} = 2a^4b^2$

packet:

1. $8^{-2} = \frac{1}{8^2} = \frac{1}{64}$

2. $-6(3^{-2})(81) = -6\left(\frac{1}{3^2}\right)81 = -6 \cdot \frac{1}{9} \cdot 81 = -6 \cdot 9 = -54$

3. $y^3y^{-7} = y^{3-7} = y^{-4} = \frac{1}{y^4}$

4. $\frac{a^{-2}b^3}{a^4b^5} = a^{-2-4}b^{3-5} = a^{-6}b^{-2} = \frac{1}{a^6b^2}$

5. $\left(\frac{c}{3}\right)^{-2} = \frac{3^2}{c^2} = \frac{9}{c^2}$

6. $(9a^{-2}b^3)^{-2} = 9^{-2}a^{(-2)(-2)}b^{3(-2)} = \frac{1}{9^2}a^4b^{-6} = \frac{a^4}{81b^6}$

7. $\frac{(x^3y^{-1})^2}{(xy^2)^{-2}} = \frac{x^{3(2)}y^{-1(2)}}{x^{(-2)}y^{2(2)}} = \frac{x^6y^{-2}}{x^{-2}y^4} = x^{6-(-2)}y^{-2-4} = x^8y^{-2} = \frac{x^8}{y^2}$

8. $\frac{3(x^2y)^3}{12(x^{-2}y)^4} = \frac{3x^6y^3}{12x^{-8}y^4} = \frac{3}{12}x^{6-(-8)}y^{3-4} = \frac{1}{4}x^{14}y^{-1} = \frac{x^{14}}{4y}$

9. $\frac{b^{-4}}{b^{-5}} = b^{-4-(-5)} = b^{-4+5} = b$

10. $\frac{12a^3b^{-4}}{4a^{-2}b} = \frac{12}{4}a^{3-(-2)}b^{(-4)-1} = 3a^5b^{-5} = \frac{3a^5}{b^5}$

11. $\left(\frac{x^{-3}y^4}{5}\right)^{-3} = \frac{x^9y^{-12}}{5^3} = \frac{5^3x^9}{y^{12}} = \frac{125x^9}{y^{12}}$

REVIEW

12. $\frac{5}{8} + \frac{11}{24} = \frac{3}{8} \cdot \frac{5}{8} + \frac{11}{24} = \frac{15}{24} + \frac{11}{24} = \frac{26}{24} \stackrel{?}{=} \frac{13}{12}$

13. $\frac{3}{3} | 2x-5 | = \frac{15}{3} \rightarrow | 2x-5 | = 5$

$$\begin{array}{r} 2x-5=5 \\ +5 \quad +5 \\ \hline 2x=10 \\ \frac{2x}{2}=\frac{10}{2} \\ \hline x=5 \end{array} \quad \begin{array}{r} 2x-5=-5 \\ +5 \quad +5 \\ \hline 2x=0 \\ \frac{2x}{2}=\frac{0}{2} \\ \hline x=0 \end{array}$$

$x=5, x=0$

14. x-intercept is 4; y-intercept is 2

$(4,0) \quad (0,2) \quad m = \frac{2-0}{0-4} = \frac{2}{-4} = -\frac{1}{2}$

$y = -\frac{1}{2}x + 2$

Book: p 52

3. $y = 3x$
 $x+21 = -2y$

$$\begin{array}{r} x+21 = -2(3x) \\ x+21 = -6x \\ -x \quad -x \\ \hline 21 = -7x \\ \frac{21}{-7} = \frac{-7x}{-7} \\ -3 = x \end{array}$$

$y = 3(-3)$
 $y = -9$

$(-3, -9)$

4. $(4a+3b = -2) \cdot 5 \rightarrow 20a + 15b = -10$
 $(5a+7b = 17) \cdot -4 \rightarrow -20a - 28b = -68$

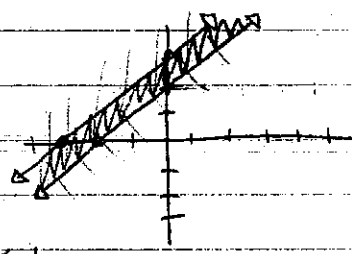
$$\begin{array}{r} 20a + 15b = -10 \\ -20a - 28b = -68 \\ \hline -13b = -78 \rightarrow b = 6 \end{array}$$

$(-5, 6)$

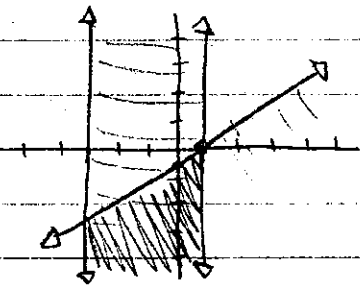
$$\begin{array}{r} 4a + 3(6) = -2 \\ 4a + 18 = -2 \\ -18 \quad -18 \\ \hline 4a = -20 \\ \frac{4a}{4} = \frac{-20}{4} \\ a = -5 \end{array}$$

p 51

(x2) 16. $y - x \leq 3$ x int: (-3, 0)
 $y \geq x + 2$ y int: (0, 3)
x int: (-2, 0)
y int: (0, 2)



(x2) 22. $|x+1| \leq 2$ $\begin{cases} x+1 \leq 2 \rightarrow x \leq 1 \\ x+1 \geq -2 \rightarrow x \geq -3 \end{cases}$
 $x - 2y \geq 1$ x int: (1, 0)
y int: (0, -1/2)



Alg 2 Assignment 16, continued

p259 $6. y^5 \cdot y^7 = y^{5+7} = \boxed{y^{12}}$

10. $\frac{-2c^3d^6}{24c^2d^2} = \frac{-2c^{3-2}d^{6-2}}{24} = \frac{-1cd^4}{12} = \boxed{\frac{-cd^4}{12}}$

24. $\frac{-x^6y^6}{x^3y^4} = -x^{6-3}y^{6-4} = \boxed{-x^3y^2}$

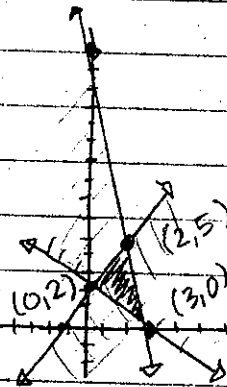
28. $(3a^3b)(-5a^2b^2) = -15a^{3+2}b^{1+2} = \boxed{-15a^5b^3}$

38. $\frac{2x^5y^3z^3}{8x^3y^7z} = \frac{1x^{5-3}y^{3-7}z^{3-1}}{4} = \frac{1x^2y^{-4}z^2}{4} = \boxed{\frac{x^2z^2}{4y^4}}$

p157: 14. $2x+3y \geq 6$ $x(3,0)$ $y(0,2)$
 $3x-2y \geq -4$ $x(-4/3,0)$ $y(0,2)$
 $5x+y \leq 15$ $x(3,0)$ $y(0,15)$

(+2)

$f(x,y) = x+3y$	
(0,2)	$0+3(2) = 6$
(3,0)	$3+3(0) = 3$
(2,5)	$2+3(5) = 17$

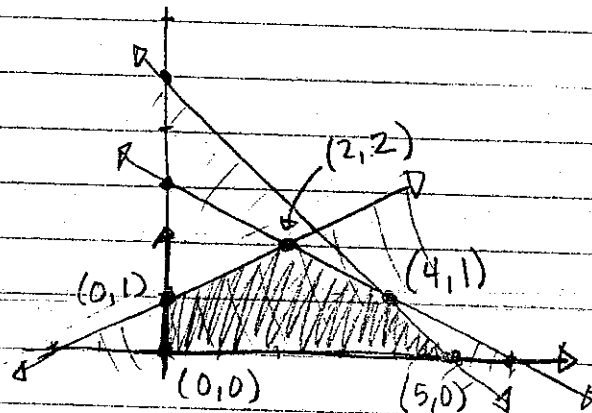


$\text{Max} = 17 \text{ at } (2,5), \text{ Min} = 3 \text{ at } (3,0)$

22. $x \geq 0$
 $y \geq 0$
 $x+2y \leq 6$ $x(6,0)$ $y(0,3)$
 $2y-x \leq 2$ $x(-2,0)$ $y(0,1)$
 $x+y \leq 5$ $x(5,0)$ $y(0,5)$

(+2)

$f(x,y) = 3x-5y$	
(0,0)	$3(0)-5(0) = 0$
(0,1)	$3(0)-5(1) = -5$
(2,2)	$3(2)-5(2) = -4$
(4,1)	$3(4)-5(1) = 7$
(5,0)	$3(5)-5(0) = 15$



$\text{Max is } 15 \text{ at } (5,0)$
 $\text{Min is } -5 \text{ at } (0,1)$

p163

6. a) $x = \text{cars}, y = \text{buses}$

$$x \geq 0, y \geq 0, x + y \leq 60, 6x + 30y \leq 600$$

(x2)

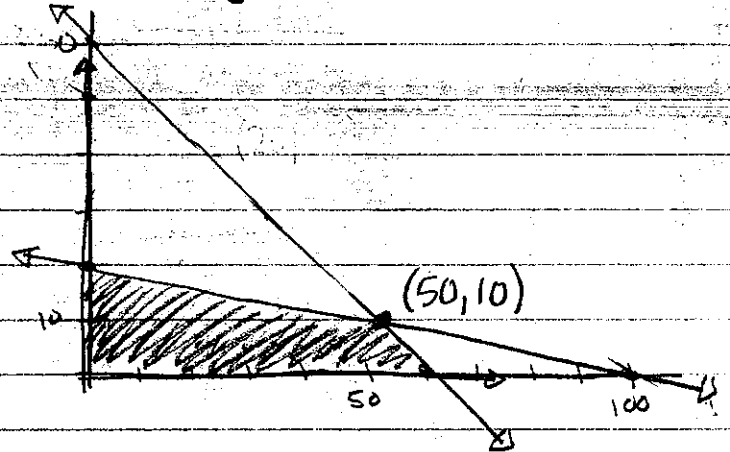
b) $f(x,y) = 2.50x + 7.50y$

$(0,0) \quad 2.5(0) + 7.5(0) = 0$

$(0,20) \quad 2.5(0) + 7.5(20) = 150$

$(50,10) \quad 2.5(50) + 7.5(10) = 200$

$(60,0) \quad 2.5(60) + 7.5(0) = 150$



Max income \$200
with 50 cars & 10 buses.

c) $f(x,y) = 4x + 8y$

$(0,0) \quad 4(0) + 8(0) = 0$

$(0,20) \quad 4(0) + 8(20) = 160$

$(50,10) \quad 4(50) + 8(10) = 280$

$(60,0) \quad 4(60) + 8(0) = 240$

Max income \$280
with 50 cars & 10 buses.

10. $x = \text{console}, y = \text{wide screen}$

(x2)

$$x \geq 0, y \geq 0, x \leq 450, y \leq 200, 600x + 900y \leq 360,000$$

$f(x,y) = 125x + 200y$

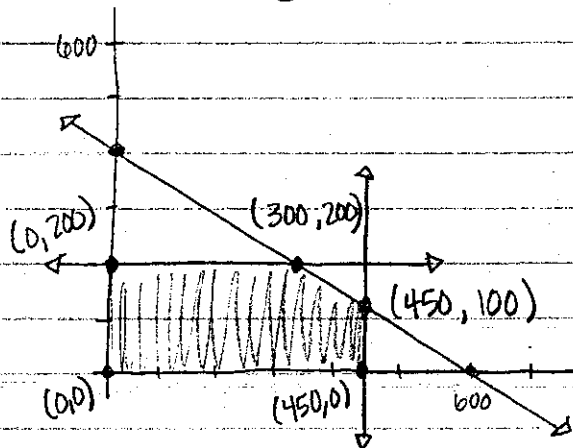
$(0,0) \quad 125(0) + 200(0) = 0$

$(0,200) \quad 125(0) + 200(200) = 40,000$

$(300,200) \quad 125(300) + 200(200) = 77,500$

$(450,100) \quad 125(450) + 200(100) = 76,250$

$(450,0) \quad 125(450) + 200(0) = 56,250$



Max profit is \$77,500
with 300 console TVs, and
200 wide-screen TVs.

Assign 1b

New

Book

pg 259: 5, 13, 25, 43

5. Write $3wz^{-4}$ without using neg. exponents

$$\frac{3w}{z^4}$$

Simplify

$$13. \left(\frac{bc}{2}\right)^{-3} = \left(\frac{2}{bc}\right)^3 = \frac{2^3}{b^3c^3} = \frac{8}{b^3c^3}$$

$$25. (a^3b^3)(ab)^{-2} = \frac{(a^3b^3)}{(ab)^2} = \frac{a^3b^3}{a^2b^2} = ab$$

$$43. \frac{40a^{-1}b^{-7}}{20a^{-5}b^{-9}} = \frac{2a^5b^9}{a^{-1}b^{-7}} = 2a^4b^2$$

Packet - Simplify

$$1. 8^{-2} = \frac{1}{8^2} = \frac{1}{64}$$

$$2. -6(3^{-2})(81) = -\frac{6}{1} \cdot \frac{1}{3^2} \cdot \frac{81}{1} = -\frac{6}{1} \cdot \frac{1}{9} \cdot \frac{81}{1} = -54$$

$$3. y^3y^{-7} = \frac{y^3}{y^7} = \frac{1}{y^4}$$

$$4. \frac{a^{-2}b^3}{a^4b^5} = \frac{b^3}{a^4a^2b^5} = \frac{b^3}{a^6b^5} = \frac{1}{a^6b^2}$$

$$5. \left(\frac{c}{3}\right)^{-2} = \left(\frac{3}{c}\right)^2 = \frac{9}{c^2}$$

$$6. (9a^{-2}b^3)^{-2} = \frac{1}{(9a^{-2}b^3)^2} = \frac{1}{81a^{-4}b^6} = \frac{a^4}{81b^6}$$

$$7. \frac{(x^3y^{-1})^2}{(xy^2)^{-2}} = \frac{x^6y^{-2}}{x^{-2}y^4} = \frac{x^6x^2y^4}{y^2} = x^8y^2$$

$$8. \frac{3(x^2y)^3}{12(x^{-2}y)^4} = \frac{1x^6y^3}{4x^{-8}y^4} = \frac{x^6x^8}{4y} = \frac{x^{14}}{4y}$$

New
Packet cont

$$9. \frac{b^{-1}}{b^{-5}} = \frac{b^5}{b^4} = \boxed{b}$$

$$10. \frac{12a^3b^4}{4a^{-2}b} = \frac{3a^3a^2}{bb^4} = \boxed{\frac{3a^5}{b^5}}$$

$$11. \left(\frac{x^{-3}y^4}{5}\right)^{-3} = \left(\frac{5}{x^{-3}y^4}\right)^3 = \frac{5^3}{x^{-9}y^{12}} = \boxed{\frac{125x^9}{y^{12}}}$$

Review

$$12. \frac{5}{8} + \frac{11}{24} = \frac{15}{24} + \frac{11}{24} = \frac{26}{24} = \boxed{\frac{13}{12}}$$

$$13. \text{Solve: } \frac{3}{2} |2x-5| = \frac{15}{3}$$

$$|2x-5| = 5$$

$$\begin{array}{r} 2x-5=5 \\ +5 \quad +5 \\ \hline 2x=10 \\ \frac{2x}{2} = \frac{10}{2} \end{array}$$

$$\begin{array}{r} 2x-5=-5 \\ +5 \quad +5 \\ \hline 2x=0 \\ \frac{2x}{2} = \frac{0}{2} \end{array}$$

$$\frac{2x}{2} = \frac{10}{2}$$

$$\frac{2x}{2} = \frac{0}{2}$$

$$x=5$$

$$x=0$$

14. Find equation in $y=mx+b$: x -int is 4, y -int is 2

$(4,0), (0,2)$

$$m = \frac{2-0}{0-4} = \frac{2}{-4} = -\frac{1}{2}$$

$$\boxed{y = -\frac{1}{2}x + 2}$$

BOOK →

Review cont.

Assign 16
cont

Book

pg 152: self test 3, 4 (no calc) - Solve Sub or elim.

$$3. \quad y = 3x$$

$$x + 21 = -2y$$

$$-x + 21 = -2(3x)$$

$$x + 21 = -6x$$

$$\begin{array}{r} +6x - 21 \\ +6x - 21 \end{array}$$

$$y = 3(-3)$$

$$y = 9$$

$$\frac{7x}{7} = \frac{-21}{7}$$

$$x = -3$$

$$\boxed{(-3, 9)}$$

$$4. \quad (4a + 3b = -2) \cdot 5 \rightarrow -20a - 15b = 10$$

$$(5a + 7b = 17) \cdot 4 \rightarrow 20a + 28b = 68$$

$$\frac{13b}{13} = \frac{78}{13}$$

$$b = 6$$

$$4a + 3(b) = -2$$

$$4a + 18 = -2$$

$$\begin{array}{r} -18 \\ -18 \end{array}$$

$$\frac{4a}{4} = \frac{-20}{4}$$

$$a = -5$$

$$\boxed{(-5, 6)}$$

pg. 151: #16, 22 (no calc) Solve system by graphing
(x-y ints)

$$16. \quad y - x \leq 3$$

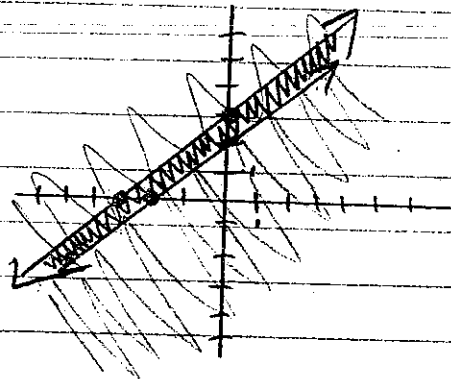
$$y \geq x + 2$$

$$x\text{-int: } (-3, 0) \quad y\text{-int: } (0, 3)$$

$$x\text{-int: } (-2, 0) \quad y\text{-int: } (0, 2)$$

$$\text{Test } (0, 0): 0 - 0 \leq 3 \quad 0 \leq 3 \quad \checkmark$$

$$\text{Test } (0, 0): 0 \geq 0 + 2 \quad 0 \geq 2 \quad \times$$



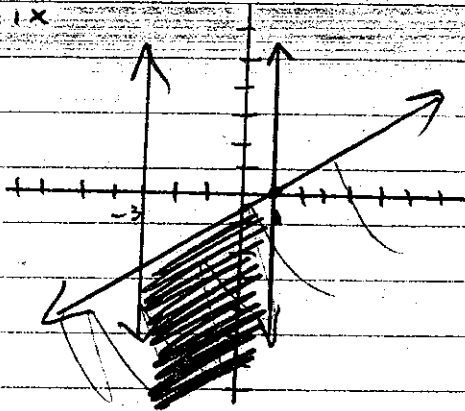
Assign 16 cont

pg 151: 16, 22 cont

22. $|x+1| \leq 2$ $x-2y \geq 1 \rightarrow x\text{-int: } (1,0), y\text{-int: } (0, -\frac{1}{2})$

$$\begin{array}{r} x+1 \leq 2 \\ \underline{-1 \quad -1} \\ x \leq 1 \end{array} \quad \begin{array}{r} x+1 \geq -2 \\ \underline{-1 \quad -1} \\ x \geq -3 \end{array}$$

Test (0,0)
 $0-0 \geq 1$
0 > 1 X



pg 259: 6, 10, 24, 28, 38 (no calc)

6. $y^5 \cdot y^7 = \boxed{y^{12}}$

10. $\frac{-2c^3d^6}{24c^2d^2} = \boxed{\frac{-1cd^4}{12} \text{ or } -\frac{1}{12}cd^4}$

24. $\frac{-x^6y^6}{x^3y^4} = \boxed{-x^3y^2}$

28. $(3a^3b)(-5a^2b^2) = \boxed{-15a^5b^3}$

38. $\frac{2x^5y^3z^3}{8x^3y^7z} = \frac{1x^2z^2}{4y^4} = \boxed{\frac{x^2z^2}{4y^4}}$

pg 157: 14, 22 (calc to find vertices if needed)

14. $2x+3y \geq 6 \rightarrow x\text{-int: } (3,0) y\text{-int: } (0,2)$

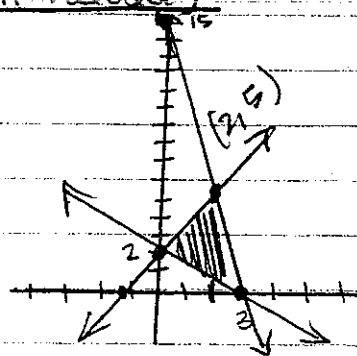
$3x-2y \geq -4 \rightarrow x\text{-int: } (-\frac{4}{3}, 0) y\text{-int: } (0,2)$

$5x+y \leq 15 \rightarrow x\text{-int: } (3,0) y\text{-int: } (0,15)$

$f(x,y) = x+3y$

The min is 3 at (3,0).
The max is 17 at (2,5).

(x,y)	$x+3y$	$f(x,y) =$
(3,0)	$3+3(0) = 3$	$f(3,0) = 3$ min
(0,2)	$0+3(2) = 6$	$f(0,2) = 6$
(2,5)	$2+3(5) = 17$	$f(2,5) = 17$ max



Assign 16 cont

pg 157: 22 cont

22. $x \geq 0$

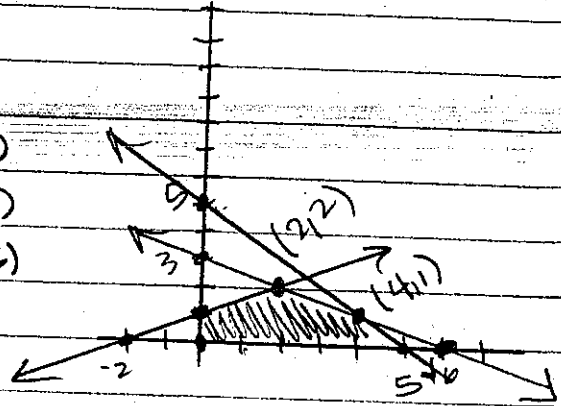
$y \geq 0$

$x + 2y \leq 6 \rightarrow x\text{-int: } (6,0) \quad y\text{-int: } (0,3)$

$2y - x \leq 2 \rightarrow x\text{-int: } (-2,0) \quad y\text{-int: } (0,1)$

$x + y \leq 5 \rightarrow x\text{-int: } (5,0) \quad y\text{-int: } (0,5)$

$f(x,y) = 3x - 5y$



(x,y)	$3x - 5y$	$f(x,y) =$
$(0,0)$	$3(0) - 5(0) = 0$	$f(0,0) = 0$
$(5,0)$	$3(5) - 5(0) = 15$	$f(5,0) = 15$ max
$(4,1)$	$3(4) - 5(1) = 7$	$f(4,1) = 7$
$(2,2)$	$3(2) - 5(2) = -4$	$f(2,2) = -4$
$(0,1)$	$3(0) - 5(1) = -5$	$f(0,1) = -5$ min

The max is 15 at $(5,0)$
The min is -5 at $(0,1)$.

pg 163: 6, 10 (calc to find vertices if needed)

6. $c = \text{cars } (x)$

$b = \text{buses } (y)$

a. $c \geq 0$

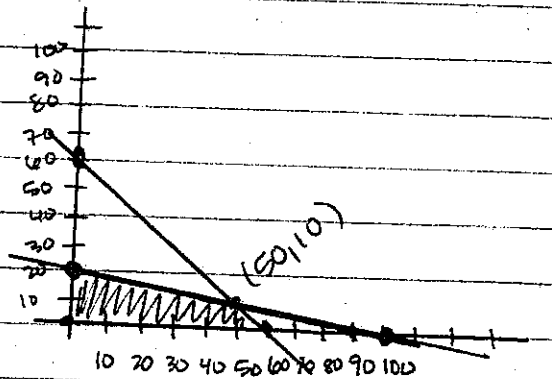
$b \geq 0$

$6c + 30b \leq 600 \rightarrow x\text{-int: } (100,0), y\text{-int: } (0,20)$

$c + b \leq 60 \rightarrow x\text{-int: } (60,0), y\text{-int: } (0,60)$

b. $f(x,y) = 2.50c + 7.50b$

(x,y)	$2.5x + 7.5y$	$f(x,y) =$
$(0,0)$	$2.5(0) + 7.5(0) = 0$	$f(0,0) = 0$
$(60,0)$	$2.5(60) + 7.5(0) = 150$	$f(60,0) = 150$
$(50,10)$	$2.5(50) + 7.5(10) = 200$	$f(50,10) = 200$
$(0,20)$	$2.5(0) + 7.5(20) = 150$	$f(0,20) = 150$



50 cars and 10 buses
should be accepted for
a max \$200 income.

10. c_0

(x,y)	$4x + 8y$	$f(x,y) =$
$(0,0)$	$4(0) + 8(0) = 0$	$f(0,0) = 0$
$(60,0)$	$4(60) + 8(0) = 240$	$f(60,0) = 240$
$(50,10)$	$4(50) + 8(10) = 280$	$f(50,10) = 280$
$(0,20)$	$4(0) + 8(20) = 160$	$f(0,20) = 160$

50 cars and 10 buses
should be accepted for
a max \$280 income.

Assign 16 cont

pg 163: 10 cont

10. $x = \text{console TV}$
 $y = \text{wide-screen TV}$

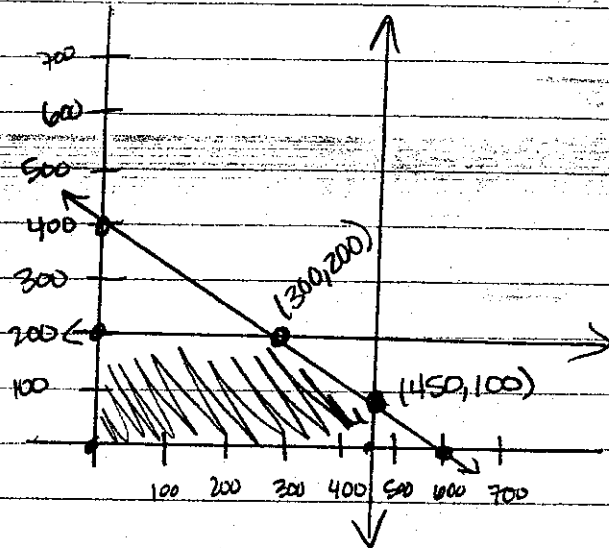
$$\begin{aligned} x &\leq 450 & x &\geq 0 \\ y &\leq 200 & y &\geq 0 \end{aligned}$$

$$600x + 900y \leq 360,000$$

$$x\text{-int: } (600, 0)$$

$$y\text{-int: } (0, 400)$$

$$y \leq \frac{(360,000 - 600x)}{900}$$



$$f(x,y) = 125x + 200y$$

(x, y)	$125x + 200y$	$f(x,y) =$
$(0, 0)$	$125(0) + 200(0) =$	$f(0,0) = 0$
$(450, 0)$	$125(450) + 200(0) =$	$f(450,0) = 56,250$
$(450, 100)$	$125(450) + 200(100) =$	$f(450,100) = 76,250$
$(300, 200)$	$125(300) + 200(200) =$	$f(300,200) = 77,500$
$(0, 200)$	$125(0) + 200(200) =$	$f(0,200) = 40,000$

To maximize profits, the company should make 300 console TV's and 200 wide-screen TV's.

The max profit is \$ 77,500.