

Algebra 2ⁿ Assignment 46

NEW

$$1. 3^{4x} = 3^{x-3} \rightarrow \frac{4x}{-x} = \frac{x-3}{-x} \rightarrow \frac{3x}{3} = \frac{-3}{3} \rightarrow \boxed{x = -1}$$

$$2. 4^x = 16 \rightarrow 4^x = 4^2 \rightarrow \boxed{x = 2}$$

$$3. 7^x = \frac{1}{49} \rightarrow 7^x = \frac{1}{7^2} \rightarrow 7^x = 7^{-2} \rightarrow \boxed{x = -2}$$

$$4. 8^x = 4 \rightarrow \log_8 4 = x \rightarrow \frac{\log 4}{\log 8} = x \rightarrow .6667 = x \rightarrow \boxed{x = \frac{2}{3}}$$

OR $2^{3x} = 2^2 \rightarrow 3x = 2 \rightarrow x = \frac{2}{3}$

$$5. \left(\frac{1}{9}\right)^m = 81^{m+4} \rightarrow 9^{-m} = 81^{m+4} \rightarrow 9^{-m} = 9^{2(m+4)}$$

$$\rightarrow -m = 2(m+4) \rightarrow -m = 2m+8 \rightarrow -3m = 8 \rightarrow \boxed{m = -\frac{8}{3}}$$

$$6. 4^{2x-7} = 64 \rightarrow 4^{2x-7} = 4^3 \rightarrow 2x-7 = 3 \rightarrow 2x = 10 \rightarrow \boxed{x = 5}$$

$$7. 2^x = 53 \rightarrow \log_2 53 = x \rightarrow \frac{\log 53}{\log 2} = x \rightarrow 5.728 = x$$

$$8. 8^{2x} = 124 \rightarrow 2x = \log_8 124 \rightarrow \frac{2x}{2} = \frac{\ln 124}{\ln 8} \rightarrow \boxed{x = \frac{\ln 124}{2 \ln 8} = 1.159}$$

$$9. 4^{x+5} = 7 \rightarrow x+5 = \log_4 7 \rightarrow x = \log_4 7 - 5 \rightarrow \boxed{x = \frac{\ln 7}{\ln 4} - 5 = -3.596}$$

$$10. 2^{x-5} = 9 \rightarrow x-5 = \log_2 9 \rightarrow x = \log_2 9 + 5 \rightarrow \boxed{x = \frac{\ln 9}{\ln 2} + 5 = 8.170}$$

$$11. e^x = 10 \rightarrow \log_e 10 = x \rightarrow \boxed{x = \ln 10 = 2.303}$$

$$12. 4e^{2x} = 5 \rightarrow e^{2x} = \frac{5}{4} \rightarrow 2x = \ln\left(\frac{5}{4}\right) \rightarrow \boxed{x = \frac{\ln\left(\frac{5}{4}\right)}{2} = .112}$$

$$13. \quad 7 - e^x = 5 \rightarrow \frac{-e^x}{-1} = \frac{-2}{-1} \rightarrow e^x = 2 \rightarrow \boxed{x = \ln 2 = .693}$$

$$14. \quad \begin{array}{r} -14 + 3e^x = 7 \\ +14 \quad \quad +14 \end{array}$$

$$\frac{3e^x}{3} = \frac{21}{3} \rightarrow e^x = 7 \rightarrow \boxed{x = \ln(7) = 1.946}$$

$$15. \quad \begin{array}{r} 9e^{5x} - 4 = 50 \\ +4 \quad \quad +4 \end{array}$$

$$\frac{9e^{5x}}{9} = \frac{54}{9} \rightarrow e^{5x} = 6 \rightarrow 5x = \ln 6 \rightarrow \boxed{x = \frac{\ln(6)}{5} = .358}$$