

34 problems
 Review # 26 and
 pg 778 #36 worth
 2 points each.

score / 36

Algebra 2 - Assignment 53 Key

NEW

1. $y = 2\sin\theta$

amplitude = 2
 period = 2π

2. $y = \cos(3\theta)$

amplitude = 1
 period = $\frac{2\pi}{3}$

3. $y = 3\cos(\frac{1}{2}\theta)$

amplitude = 3
 period = $\frac{2\pi}{1/2} = 2\pi(2) = 4\pi$

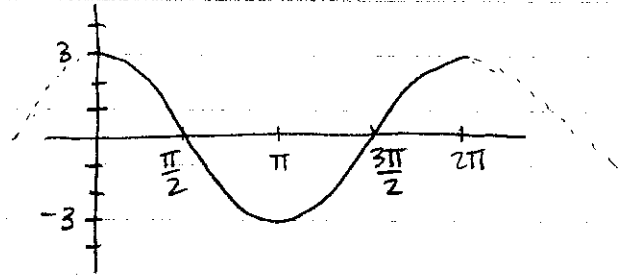
4. $y = 5\sin(\frac{\pi}{5}\theta)$

amplitude = 5
 period = $\frac{2\pi}{\pi/5} = 2\pi \cdot \frac{5}{1} = 10$

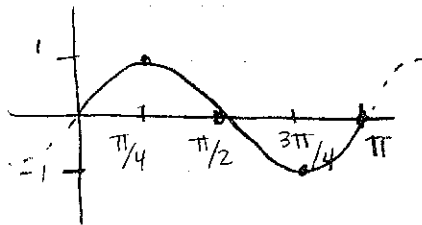
5. $y = 6\sin(\frac{2}{3}\theta)$

amplitude = 6
 period = $\frac{2\pi}{2/3} = 2\pi \cdot \frac{3}{2} = 3\pi$

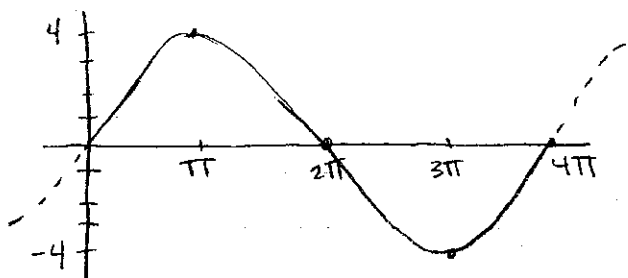
6. $y = 3\cos x$
 amp = 3
 period = 2π



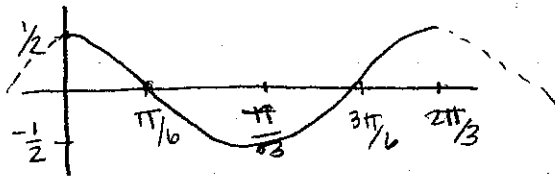
7. $y = \sin 2x$
 amp = 1
 period = $\frac{2\pi}{2} = \pi$



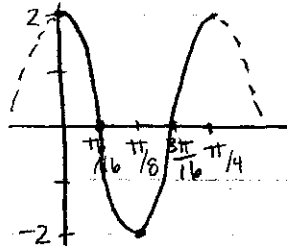
8. $y = 4\sin(\frac{1}{2}x)$
 amp = 4
 period = $\frac{2\pi}{1/2} = 2\pi \cdot 2 = 4\pi$



9. $y = \frac{1}{2} \cos 3x$
 amp = $\frac{1}{2}$
 period = $\frac{2\pi}{3}$



10. $y = 2 \cos 8x$
 amp = 2
 period = $\frac{2\pi}{8} = \frac{\pi}{4}$



REVIEW

11. Solve: $\sqrt{x-8} + \sqrt{x} = 4$

$$\begin{aligned} \sqrt{x-8} &= 4 - \sqrt{x} \\ \sqrt{x-8}^2 &= (4 - \sqrt{x})^2 \\ x-8 &= 16 - 4\sqrt{x} - 4\sqrt{x} + x \end{aligned}$$

$$\frac{-24}{-8} = \frac{-8\sqrt{x}}{-8}$$

$$\begin{aligned} 3 &= \sqrt{x} \\ 3^2 &= \sqrt{x}^2 \\ \boxed{9} &= x \end{aligned}$$

12. Solve by quad rat formula: $4x^2 - 8x + 13 = 0$

$$x = \frac{8 \pm \sqrt{64 - 4(4)(13)}}{2(4)} = \frac{8 \pm \sqrt{64 - 208}}{8} = \frac{8 \pm \sqrt{-144}}{8}$$

$$= \frac{8 \pm 12i}{8} = \boxed{\frac{2 \pm 3i}{2}}$$

$$\begin{array}{r} 16 \\ 13 \\ \hline 48 \\ 16 \\ \hline 208 \end{array}$$

13. $2 \log_3 x - \log_3 (x-2) = 2$

$$\log_3 \left(\frac{x^2}{x-2} \right) = 2 \rightarrow \frac{x^2}{x-2} = 3^2 \rightarrow x^2 = 9x - 18$$

$$\rightarrow x^2 - 9x + 18 = 0 \rightarrow (x-6)(x-3) = 0 \rightarrow x-6=0 \quad x-3=0$$

$$\boxed{x=6, x=3}$$

14. $\log_6 x = \frac{3}{2} \log_6 9 + \log_6 2$

$$\log_6 x = \log_6 (9^{3/2} \cdot 2)$$

$$x = 27 \cdot 2$$

$$\boxed{x = 54}$$

Asmt 53 - continued

15. $\cos \frac{\pi}{4} = \frac{\sqrt{2}}{2}$

16. $\tan \frac{2\pi}{3} = \frac{\frac{13}{2}}{-\frac{1}{2}} = -13$

17. $\sin \frac{7\pi}{6} = \frac{-1}{2}$

18. $\sin 90^\circ = 1$

19. $\cos 135^\circ = -\frac{\sqrt{2}}{2}$

20. $\widehat{AB} = 2\left(\frac{\pi}{3}\right) = \frac{2\pi}{3}$

21. $\widehat{CA} = 2\left(\frac{2\pi}{3}\right) = \frac{4\pi}{3}$

22. radius = 15 in, arc length = 4 in

$4 = 15\theta \rightarrow \theta = \frac{4}{15}$

23. $r = 4 \text{ cm}$ $\theta = \frac{\pi}{7}$

Area = $\frac{1}{2}\left(\frac{\pi}{7}\right)4^2 = \frac{16\pi}{14} = \frac{8\pi}{7} \text{ cm}^2$

24. $r = 7 \text{ km}$ $\theta = \frac{2\pi}{5}$

Area = $\frac{1}{2}\left(\frac{2\pi}{5}\right)7^2 = \frac{49\pi}{5} \text{ km}^2$

25. $1000e^{5x} = 75$

$e^{5x} = \frac{75}{1000} \rightarrow 5x = \ln(.075) \rightarrow x = \frac{\ln(.075)}{5} = -.518$

26. $\frac{1}{2}$ life is 32 years. $p = 25 \text{ g}$

(2pts) a) $y = 25e^{(-\ln 2/32)(10)} = 20.13 \text{ g.}$

b) $10 = 25e^{(-\ln 2/32)t} \rightarrow \frac{10}{25} = e^{(-\ln 2/32)t} \rightarrow \ln\left(\frac{10}{25}\right) = \left(\frac{-\ln 2}{32}\right)t$

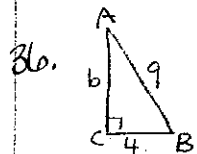
$\rightarrow t = \frac{\ln\left(\frac{10}{25}\right)}{\left(\frac{-\ln 2}{32}\right)} = 42.30 \text{ years}$

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24. $\tan(17.5) = \frac{x}{23.7} \rightarrow x = 23.7(\tan(17.5)) = \boxed{7.5}$

28. $\tan x = 0.5923 \rightarrow x = \tan^{-1}(0.5923) = 30.63 = \boxed{31^\circ}$

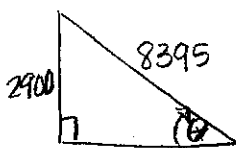
(2 pts)



$4^2 + b^2 = 9^2 \rightarrow b = \sqrt{9^2 - 4^2} = 8.1$
 $\sin \angle A = 4/9 \rightarrow \angle A = \sin^{-1}(4/9) = 26^\circ$

$\angle A = 26^\circ$	$a = 4$
$\angle B = 64^\circ$	$b = 8.1$
$\angle C = 90^\circ$	$c = 9$

52.



$\sin \theta = \frac{2900}{8395}, \theta = \sin^{-1}\left(\frac{2900}{8395}\right) = \boxed{20.2^\circ}$

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28. $\frac{3600^\circ}{20} \cdot \frac{\pi}{180} = \boxed{20\pi \text{ radians}}$

36. $3.5 \cdot \frac{180}{\pi} = \boxed{\frac{630^\circ}{\pi}}$

$$\begin{array}{r} 180 \\ 3.5 \\ \hline 900 \\ 540 \\ \hline 6300 \end{array}$$

38. -120°
 positive: $-120^\circ + 360^\circ = \boxed{240^\circ}$
 negative: $-120^\circ - 360^\circ = \boxed{-480^\circ}$

46. $-\frac{8\pi}{3}$
 negative: $-\frac{8\pi}{3} + \frac{6\pi}{3} = \boxed{-\frac{2\pi}{3}}$
 positive: $-\frac{2\pi}{3} + \frac{6\pi}{3} = \boxed{\frac{4\pi}{3}}$